#### UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN

### Microwave cavities

Physics 401, Fall 2016 Eugene V. Colla



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## Agenda

- Waves in waveguides
- Standing waves and resonance
- Setup
- Experiment with microwave cavity
- Comments on Bragg diffraction experiment



### **Reminder: Propagation of Plane Waves**



### **Wave Propagation in Wave Guides**



### **Standing Waves in Cavities**

![](_page_4_Figure_1.jpeg)

![](_page_4_Picture_2.jpeg)

![](_page_4_Picture_3.jpeg)

### **Standing Waves in Cavities**

![](_page_5_Figure_1.jpeg)

### **Resonances for transverse Electric Waves**

$$\omega_{mnp}^{2} = v_{0}^{2} \left[ \left( \frac{m\pi}{a} \right)^{2} + \left( \frac{n\pi}{b} \right)^{2} + \left( \frac{p\pi}{c} \right)^{2} \right]$$

 $v_0^2$  -phase velocity

![](_page_6_Figure_3.jpeg)

TE<sub>101</sub> mode: m=1, n=0, p=1

$$\omega_{101}^2 = v_0^2 \pi^2 \left[ \left(\frac{1}{a}\right)^2 + \left(\frac{1}{c}\right)^2 \right]$$

![](_page_6_Picture_6.jpeg)

### **Equivalent Circuit**

![](_page_7_Figure_1.jpeg)

### **Coupling between Wave Guide and Cavity**

![](_page_8_Figure_1.jpeg)

![](_page_8_Figure_2.jpeg)

Maximum power transfer:  $Z_0 = R \rightarrow \beta = 1$ 

$$\Rightarrow Q_L = \frac{1}{2}Q_0 ,$$

 $Q_0$  - quality factor without external load

![](_page_8_Picture_6.jpeg)

## Microwaves in Cavities. Overview of the Experiment.

![](_page_9_Picture_1.jpeg)

![](_page_9_Picture_2.jpeg)

Gunn diode MW oscillator

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### Microwaves in Cavities. The Setup of the Experiment.

![](_page_10_Picture_1.jpeg)

![](_page_10_Picture_2.jpeg)

### **Experiment. Wavelength measurement.**

![](_page_11_Picture_1.jpeg)

### Use detector to find distance between minimums in the slotted line (wave guide)

![](_page_11_Picture_3.jpeg)

### **Experiment. Wavelength measurement.**

![](_page_12_Figure_1.jpeg)

Use detector to find distance between minimums in the slotted line (wave guide). Distance between consequent minima correspond  $\lambda/2$ 

![](_page_13_Figure_1.jpeg)

![](_page_13_Picture_2.jpeg)

$$\omega_{102}^2 = v_0^2 \pi^2 \left[ \left(\frac{1}{a}\right)^2 + \left(\frac{2}{c}\right)^2 \right] \qquad \longrightarrow \qquad f_{102} = \frac{v_0}{2} \sqrt{\left[ \left(\frac{1}{a}\right)^2 + \left(\frac{2}{c}\right)^2 \right]}$$

![](_page_14_Figure_2.jpeg)

![](_page_14_Picture_3.jpeg)

![](_page_15_Figure_1.jpeg)

![](_page_16_Figure_1.jpeg)

![](_page_16_Picture_2.jpeg)

- 1. Oscilloscope should run in X-Y mode
- 2. To plot the I(f) dependence you have to download both Ch1 and Ch2 data
- 3. Use triangular waveform as a voltage applied to modulation input of the oscillator
- 4. Use a proper time scale setting on the scope which could estimated from scanning frequency
- 5. Apply the calibration equation to calculate the frequency of the oscillator from the modulation voltage

-		<u> </u>	"2 "1 <b>"P I L</b>	· · · · · · · ·			
1		A(X)	B(Y)	C(Y)	D(Y)	E(Y) 💩	
	Long Name	time	1	time	Vmod	f	
	Units	s	A	S	V	GHz	
	1	0	****	0	3.85055	3.0776	
	2	1E-6	****	1E-6	3.84992	3.07758	
	3	2E-6	****	2E-6	3.84578	3.07742	
	4	3E-6	*****	3E-6	3.84297	3.07732	
						<i>f</i> =	$= 0.03706 V_{mod} + 2.9349$

![](_page_18_Picture_1.jpeg)

Voltage tunable oscillator ZX95-3250a-S+ from

#### **Mini-Circuits**<sup>®</sup>

![](_page_18_Picture_4.jpeg)

#### FM Calibration for microwave oscillator

![](_page_19_Figure_2.jpeg)

#### ZX95-3250a-S+

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![](_page_20_Figure_1.jpeg)

By changing of the coupling between oscillator and cavity we can control the quality factor of the cavity resonance but in the same time we changing the power delivered to the cavity

![](_page_21_Figure_2.jpeg)

### Experiment. Coupling: Detecting of the Magnetic field.

![](_page_22_Picture_1.jpeg)

![](_page_22_Figure_2.jpeg)

While in resonance: turn orientation of the input loop from the vertical direction in 10° steps to 360°. Read cavity detector.

![](_page_22_Picture_4.jpeg)

## Experiment. Coupling: Detecting of the Magnetic field.

![](_page_23_Figure_1.jpeg)

10/31/2016

### **Electric Field Distribution.**

![](_page_24_Figure_1.jpeg)

Presence of dielectric reduces length of cavity at a given resonance frequency  $\omega_0$ .

This effect grows with the electric field strength E<sub>y</sub>.

- (0) Without dielectric the cavity length at resonace is  $c_0$ .
- (1) Place dielectric into cavity and move in 0.5cm steps,  $I_{i}$ .
- (2) At each place tune plunger to resonance and record  $c_i$ .
- (3) Plot  $\Delta c_i = |c_0 c_i|$  versus  $I_i$ : this measures now  $E_y$  vs I!

### **Electric Field Distribution.**

![](_page_25_Figure_1.jpeg)

#### **Courtesy of P. Debevec**

![](_page_25_Picture_3.jpeg)

### Calculation of the Quality factor of the Unloaded Cavity

**Quality factor (TE<sub>101</sub> mode) of unloaded cavity can be calculated as:** 

$$Q_0 = \frac{abc(a^2 + c^2)}{\delta \left[2b(a^3 + c^3) + ac(a^2 + c^2)\right]}$$

 $\delta$  is the skin depth at frequency  $\omega_{0}$ 

![](_page_26_Figure_4.jpeg)

$$\delta = \sqrt{2\rho / \mu \omega}$$

ρ – resistivity of the cavity material μ=μ<sub>r</sub>μ<sub>0</sub>≈μ<sub>0</sub>=4πx10<sup>-7</sup>

### Calculation of the Quality factor of the **Unloaded Cavity**

For red brass  $\rho = 6 \times 10^{-8} \Omega m$ µ≈4π**x**10<sup>-7</sup>

$$\delta = \sqrt{2\rho / \mu \omega}$$

δ=2.25x10<sup>-6</sup>m

a=7.22 cm, b=3.42 cm, c=6.91 cm (TE<sub>101</sub>)

![](_page_27_Figure_5.jpeg)

### Bragg diffraction.

![](_page_28_Figure_1.jpeg)

**θ'=90**<sup>0</sup>-θ

![](_page_28_Figure_3.jpeg)

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#### **Bragg diffraction. Results.\***

![](_page_29_Figure_1.jpeg)

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### Bragg diffraction. Possible origin of the ~10<sup>o</sup> peak

![](_page_30_Figure_1.jpeg)

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